Model reference-based machining force and surface roughness control

F. Cus, U. Zuperl*
Faculty of Mechanical Engineering, University of Maribor,
Smetanova 17, 2000 Maribor, Slovenia
* Corresponding author: E-mail address: uros.zuperl@uni-mb.si

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ABSTRACT

Purpose: The main objective of this paper is to present the development of an empirical model-based control mechanism to maintain a fine surface finish quality by maintaining on-line cutting values.

Design/methodology/approach: The proposed model has been developed to present the control model constraints, by varying the machining parameters to control the force output to be constant. Genetic programming method (GP) has been applied to derive empirical relationship of the surface finish and the cutting force. These relationships have been applied to develop the proposed simulation model, in which the cutting force is adjusted to improve the required surface finish for the end milling operation process.

Findings: The experimental results show that not only does the milling system with the design controller have high robustness, and global stability but also the machining efficiency of the milling system with the adaptive controller is much higher than for traditional CNC milling system. Experiments have confirmed efficiency of the adaptive control system, which is reflected in improved surface quality and decreased tool wear.

Research limitations/implications: The proposed architecture for determining of optimal cutting conditions is applied to ball-end milling in this paper, but it is obvious that the system can be extended to other machines to improve cutting efficiency.

Practical implications: The results of experiments demonstrate the ability of the proposed system to effectively regulate peak cutting forces for cutting conditions commonly encountered in end milling operations. The high accuracy of results within a wide range of machining parameters indicates that the system can be practically applied in industry.

Originality/value: By the GP modeling the system for adaptive adjustment of cutting parameters is built.

Keywords: Machining; Model-based control system; Genetic programming

1. Introduction

The control of milling processes is presently receiving significant attention due to potential economic benefits associated with automated machining [1]. Milling processes are interesting from a control perspective due to difficulties such as system nonlinearities, time-varying parameters and tool wear [2,3]. Control techniques that have been developed for machining traditionally require some form of parameter adaptation [1,4]. Solution to this problem is adaptive control. Adaptive control system is introduced in cutting process by Stute and Goetz [5]. The most frequently used systems are MRAC (Model Reference Adaptive Control) [6] and STR (Self Tunning Regulations) [7]. MRAC, developed from adaptive control theory, is widely used for its robustness and disturbance rejection capability. Numerous forms of MRAC system have been developed [8,9].

Another solution to this problem are some intelligent control strategies [1]. The drawback of intelligent strategies is that neural network and genetic algorithm based calculation takes time, so it limits the response of the intelligent control system. In spite of initial difficulties in the development a trend towards equipping the CNC milling machine with modern adaptive systems can be noticed. For effective automatization, where the process takes place without interference of the human, continuous monitoring
of the milling process is necessary. Most frequently that is materialized by measuring the cutting forces because they contain most information about the process and the tool condition. By analyzing the cutting force characteristics it is possible to assess the changes of the quality of surface finish [10]. The abovementioned facts are the bases for the development of the model based system for dynamic adjusting and optimization of cutting parameters (SDNRP). That is an adaptive system of control which controls the cutting force and maintains constant roughness of the machined surface during milling by continuous dynamic adjustment of the cutting parameters. Within the frame of the research a simulation model for testing of stability and harmonizing of parameters of the adaptive system (SDNRP), has been developed. The SDNRP changes its reactions in response to disturbances and changes in the dynamics of the cutting process. After execution of simulations the system SDNRP is fully ready and harmonized for the use in real milling process. The simulation diagram of the proposed system is presented in section 5.

2. Model based milling process control

Model based control system is a regulator that can modify its behaviour in response to change in the dynamics of the process and the disturbances. If the cutting force maintained constant during the process of machining process, then the surface finish also remain stable. In the previous research work [11] the cutting force resultant is obtained using a Kistler force Transducer, which provides of three orthogonal components of dynamics forces F_x, F_y, F_z and these forces were measured on-line using LabView software. These measured cutting force signals are used in model controller to regulate the cutting force. The main objective of this research is to develop genetic model based control system, which can solve such difficult machining control problems.

The objective of the proposed control system is to regulate the milling process operation parameters such as the feed rate and the spindle speed, and maintain the cutting force constant, to achieve on-line the required value of the surface finish. The Heller BEA01 milling machine was used in connection with the fees drive controller

3. CNC machine feed drive system

The tests were carried out on the CNC milling machine Heller. That is a four-axes machine tool allowing 3 translations along the X, Y and Z- axis and rotation of machine table in the horizontal plane. It is fitted with CNC controls FAGOR 8040-M. Feeding axles are driven through ball screw drives by AC servomotors synchronized with permanent magnets. The type of the servo-drive is: Heller S 044/82 8-A20-2220-001/02C. The block diagram (simulation model) of the feeding servo-system is shown in Figure 1.

4. GP based models of cutting quantities

Learning of models of cutting quantities is effected with experimental results stated in previous researches [12]. The purpose of models is to define functional dependences between the influencing cutting parameters: spindle speed, surface roughness and cutting force. The genetic programming (GP) method is used for the determination of mutual relations between the rotating speed and feeding and between cutting force and roughness. In case of GP the result is the mathematical formula consisting of a series of prescribed operations.

In simulations the GP models are used because, in the simulation package Simulink, they can be easier transformed into the block recording. 185 experimental data are used to develop each genetic model. The experimental datum contains the value of the predicted (modelled) quantity and the appurtenant influencing parameters (cutting parameters). On the basis of the input and experimental data and with selected series of calculation operations the models: K1, K2, K3, K4, K5 = K6 are generated. The series of the following basic calculation operations \( F = \{+, \cdot, *, u', \ln\} \) and arguments \( \mathcal{P} = \{2, 2, 3, 2\} \) is selected. The set of terminals \( \mathcal{T} \) is given beside the block diagram of the individual model. Usually, the set of terminals consists of input data and variables of the system.

The size of the population of organisms \( M = 1500 \) and the number of generations \( G = 100 \) have been selected for the determination of the model of cutting (K4). On other models \( M = 850 \) and \( G = 100 \). The standard genetic operations of reproductions, crossover and mutation have been used. The reproduction probability \( p_r = 0.15 \), the crossover probability \( p_c = 0.5 \) and the mutation probability \( p_m = 0.1 \). The development of the model is stopped when the prescribed number of generations has been reached or when fitness of the organism is more than 97 %.

4.1. Derived GP models of cutting quantities

Prior to any machining the required quality of the surface finish \( (R_a) \) is known. The equation herebelow gives the cutting force \( (F_d) \) with which the required surface roughness is reached and maintained. For the model parameter \( F_d \) the following formula has been formed according to the GP method:

\[
F_d = 293 - \frac{593}{\sqrt{39.37 \cdot R_a}}
\]  

(1)

The following two GP models are in use for the determination of optimum cutting parameters:

\[
f = 25.4 \cdot \left(189 - \frac{5926160}{F^2}\right)
\]  

(2)

\[
n = \sqrt{(30064193 - 2.28 \cdot F^3)}
\]  

(3)

Where: \( f \) – feed rate [mm/min], \( n \) – spindle speed [min⁻¹].

The parameters with which the required surface roughness \( (R_a) \) is assured are determined according to the above equations. The objective of the SDNRP is to assure constant cutting force \( F \). The following formula (model parameter \( K4 \)) is used for simulation of the cutting process.

\[
F = 286.44 - \left(\frac{5.82 \cdot 10^{10}}{10^{10}}\right) \cdot n^3 - 8973 \cdot \ln(0.039 \cdot f)\]
\]  

(4)
Surface roughness is tested according to the following equation:

\[ R_a = 0.0254 \left( \frac{293 - F}{593} \right)^2 \]  

(5)

Where: \( R_a \): surface roughness [\( \mu \text{m} \)], \( F \): cutting force [N].

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**5. Simulator of SDNRP**

The block diagram of the simulator of the SDNRP is shown in Figure 2. If in the block diagram the model K4, the simulation model of the feed servo-drive and the model of main spindle rotation are replaced by the real machine tool, a harmonized system for dynamic adjustment of cutting conditions, ready for
Maximal cutting force, \( A \), in guides and a set of terminals: standard set of blocks in the programme package Matlab 6.5. The appurtenant cutting force \( F \) is expressed by the transfer function derived according to equation 2.

Hereinafter, the transfer functions of the individual elements of the SDNRP and the flow of signals between them are presented in detail.

K1: Figure 4 shows the transfer function defining the dependence between the desired surface roughness and the appurtenant cutting force \( F \). The transfer function is given in the form of the block diagrams. Modelling is effected with the standard set of blocks in the programme package Matlab 6.5. The set of terminals: \( \mathcal{F} = \{ R_a, F, \mathcal{H} \} \) is used. \( \mathcal{H} \) - real number at the interval from -10 to 10.

K2: Transfer function for prediction of optimum feeding \( f_a \) is derived according to equation 2. Figure 5 shows its block diagram. \( \mathcal{F} = \{ F, f_a, \mathcal{H} \} \).

K3: The relation between cutting force \( F \) and the command signal \( n_a \) is expressed by the transfer function derived according to equation 3. The transfer function is shown in Figure 6. Its purpose is to generate continuously the command signal of the rotating speed \( n_a \). \( \mathcal{F} = \{ F, n_a, \mathcal{H} \} \).

K4: The transfer function presented in Figure 7 represents the simulation model of the cutting process. By the block diagram the value of the actual cutting force on the tool cutter with given cutting conditions is predicted. \( \mathcal{F} = \{ n_a, f_a, F, R \} \).

K5, K6: By the block diagram it is tested whether the simulated \( R_a \) corresponds with the desired \( R_a \). The test procedure is shown in Figure 8. \( \mathcal{F} = \{ F, R_a, \mathcal{H} \} \).

During the machining process undesirable vibrations and disturbances occur. They are caused by: nonhomogeneity of the base material, tool wear, tool damages, defects in guides and bearings of the machine etc. By introducing the random disturbances into the simulation the stability and robustness of the proposed control system are tested. In the simulation model the unmodeled dynamics of the process is generated by random values corresponding with oscillations of the measured cutting forces. The diagram in Figure 9 simulates the unmodeled dynamics of the machine and process.

During the simulation the following values are drawn in the diagrams of the control console:
- Actual surface roughness,
- Surface roughness with the considered machine tool dynamics
- Maximal cutting force,
• Maximal cutting force with the dynamical component,
• Actual feeding,
• Actual spindle speed.

Unmodeled process dynamics

Oscilloscop

F

Fig. 9. Block diagram for relation cutting force – spindle speed nc

5.1. The realization course of SDNRP simulation

The SDNRP capacity is tested by simulations. The Matlab simulation package Simulink has been used. The simulation is initiated by the adjustment of the reference value \( R_a \) afterwards desired cutting force \( F_d \) is predicted according to the model \( K_1 \). When the force \( F_d \) is known, the values \( F_c \) and \( n_c \) are calculated within a moment according to the model \( K_2 \) and \( K_3 \). The dynamic response of the servo-system to the signal \( f_c \) is simulated by the block diagram given in Figure 1. The two transfer functions of the servo-systems generate the actual feeding \( (f_a) \) and speed \( (n_a) \) so that the cutting force, predicted according to model \( K_4 \), is constant. The simulated \( R_a \) is determined by the transfer function of the model \( K_5 \).

![Fig. 10. Dynamical adjusting of feed rate during simulation](image)

![Fig. 11. Dynamical adjusting of spindle speed during simulation](image)
The course of cutting force with dynamical adjusting of cutting parameters is shown in Fig. 13. The maximum cutting force was reduced from 430.4 mm/min to 324.6 mm/min. The optimum final spindle speed is 80 m/min. The system is changing the cutting parameters according to the simplified transfer function, which is mathematically derived on the basis of the servo-system which functions according to the simplified transfer function. The latter is mathematically derived on the basis of the model of the milling cutter. The simulations confirm that the proposed system is efficient for improving the surface quality and for maintaining constant maximum cutting force of 177.7 N. The criterion for efficiency of the system is the difference between the desired and simulated roughness, which is acceptable if not higher than 1.1 µm. The simulations indicate that the proposed system is efficient in fine machining; this is particularly favourable, since it considerably the responsiveness of the system. Moreover, the proposed system can be used in different requirements of the surface quality are tested.

The analysis of the results shows that by continuous adjusting of cutting parameters the required roughness is assured with maximum allowable tool loading. The simulations confirm that the SDNRP is efficient in fine machining; this is particularly favourable, since it considerably the responsiveness of the system. Moreover, the proposed system can be used in different requirements of the surface quality are tested.

Fig. 12. The course of cutting force without application of SDNRP

Fig. 13. The course of cutting force with dynamical adjusting of cutting parameters

Fig. 14. Surface roughness before using proposed control system
6. An example of realized SDNRP

Hereinafter, the simulation No. 5 (Table 2), effected for material Ck45 and milling cutter R216-16B20-040, is presented. The selected reference roughness is 0.81 μm. The starting optimum cutting parameters are determined by the PSO (Particle Swarm Optimization) algorithm [3]. They are given in Table 1. The simulation result is shown in the block diagram of Figure 2. The initial value of feeding is 430.4 mm/min. The system is changing that value, until optimum feeding 324.6 mm/min has been reached. The optimum final spindle speed is 2134 min⁻¹. Dynamic adjustment of feeding and spindle speed is a prerequisite for maintaining constant maximum cutting force of 177.7 N. The simulation result is the roughness 0.79 μm which is acceptable if compared with the desired value 0.81 μm (Figure 15).

Table 1.
Initial starting cutting conditions

| \( v_c \) = 80 m/min | \( R_D \) = 3 mm |
| \( f \) = 430.4 mm/min | \( A_D \) = 2 mm |

The process of simulation is shown in Figure 10 and Figure 11. It can be seen that by continuous adjusting of cutting parameters the required roughness is assured with maximum allowable tool loading.

7. Analysis of the results

By simulation the efficiency and stability of the SDNRP with different requirements of the surface quality are tested.

The criterion for efficiency of the system is the difference between the desired and simulated Ra. The starting cutting parameters and the desired Ra are the input data. In Table 2 the requirements and the results of simulations are indicated. 10 simulations have been carried out.

The simulation results (Table 2) confirm that the SDNRP is efficient in the control of the tool loading and surface roughness. It is efficient in fine machining; this is particularly favourable, since it is intended for the operations of end milling with shank end mills, where the requirements for the quality of machining are strict.

In machining, where the roughness exceeds 1.1 μm, the responsiveness of the system is slowed down. Its sensitivity for reaching the desired roughness is reduced.

Figure 12 shows the progress of the maximum cutting force without the use of the SDNRP. In this case the roughness has a random trend (Figure 14). The dynamic component of the cutting force is simulated by the block diagram in Figure 9.

The simulation graphs show that on the basis of the signals of maximum cutting force the quality of surface can be supposed. Both values are mutually related and have identical trends. The SDNRP assures constant roughness throughout machining.

The simulations confirm that the proposed system is efficient for assuring the required roughness and maintaining the constant machine loading. The control system responds to the rise of the cutting force by immediate reduction of feeding; as a result, the cutting force drops to the reference value level (Figure 13).

Constant cutting loadings lead to better quality of surface and prevent undesirable vibrations and deflections of the cutting tool. Improvement of the surface quality is most obvious in machining of corners, pockets, slots and curved surfaces, where the system prevents undesirable milling cutter deflections by reduction of feeding.

The system deals with fast changes of the cutting circumstances slightly worse due to its complex structure and errors in modeling. The reason for slow responsiveness and inaccuracy must be traced also to the manner of development of the simulation model of the feeding servo-system.

The SDNRP simulator incorporates the model of the feeding servo-system which functions according to the simplified transfer function. The latter is mathematically derived on the basis of the maker’s specifications [15]. By experimental capturing of the dynamics of the feeding servo-system it is possible to improve considerably the responsiveness of the system.

8. Conclusions

The paper presents the model based system of dynamic adjusting of cutting parameters. By dynamic adaptation of feeding and spindle speed the system controls the surface roughness and the cutting forces on the milling cutter.
Table 2. Simulation experimental results

<table>
<thead>
<tr>
<th>Sim no.:</th>
<th>Desired surface roughness $R_a$ [μm]</th>
<th>Initial cutting conditions before simulation $[13,14]$</th>
<th>Servo drive system after 15s</th>
<th>Produced surface finish $R_a$ [μm]</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$F_d$ [N] $f_c$ [mm/min] $n_c$ [min$^{-1}$]</td>
<td>$F$ [N] $f_c$ [mm/min] $n_c$ [min$^{-1}$]</td>
<td>$R_a$ [μm]</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>0.38 161.4 357.12 1974</td>
<td>166.5 264.92 2443</td>
<td>0.50</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>0.51 166.67 379.98 1895</td>
<td>169.9 282.19 2356</td>
<td>0.58</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>0.64 172.1 414.53 1704</td>
<td>173.0 297.94 2272</td>
<td>0.66</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>0.76 176.8 435.26 1563</td>
<td>175.9 313.94 2189</td>
<td>0.74</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>0.81 178.5 430.41 1571</td>
<td>177.7 324.61 2134</td>
<td>0.79</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>0.89 180.9 462.19 1437</td>
<td>178.6 329.95 2108</td>
<td>0.81</td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>1.02 184.7 485.14 1377</td>
<td>181.6 350.52 2007</td>
<td>0.91</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>1.14 188.1 507.75 1270</td>
<td>183.9 355.60 1925</td>
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<td></td>
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<tr>
<td>9</td>
<td>1.27 191.2 539.24 1116</td>
<td>185.7 381.25 1880</td>
<td>1.05</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>1.52 196.8 592.58 825</td>
<td>195.2 411.99 1716</td>
<td>1.18</td>
<td></td>
</tr>
</tbody>
</table>

The correlation between the surface roughness and the cutting forces is determined by the GP method. By simulations the adequacy and stability of the control system are confirmed. It has been proved that the surface roughness which is an important indicator of the process quality can be successfully controlled by the control of cutting forces.

By maintaining constant cutting force constant quality of surface finish is assured. On the basis of results of numerous simulations it has been decided to realize experimentally the described system of control.

The system has been conceived for the end milling operation, although it can be modified for all process of machining by cutting. It eliminates the problems related to assurance of quality of machining, efficiency of machining and prevention of tool damages.

References


